

UNIVERSITY OF ILLINOIS
AT URBANA-CHAMPAIGN

Instrumental Variables



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Outline for the Session

1. When is the treatment exogenous?
2. When is the treatment endogenous?
3. What is an IV and how does it work?
4. Operationalizing IVs
5. Source of IVs



When is the Treatment Exogenous?



Exogenous Treatment

- Exogeneity of a treatment relies on two assumptions:
 - SUTVA
 - Ignorability/Unconfoundedness: $(Y_i^T, Y_i^C) \perp T$
- Random assignment of treatment insures that treatment is independent of outcome. Thus, treatment and control groups are the same and any selection bias is erased



When is the Treatment Endogenous?



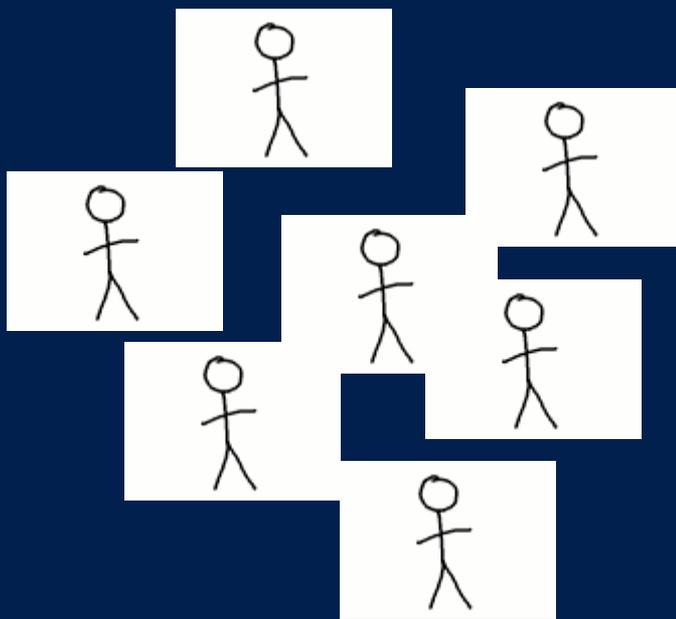
The Potential Outcomes Approach

- When our randomized design is either an encouragement design or we have imperfect compliance
 - In this case, actual treatment (T) is distinct from the variable that is randomly manipulated (Z)
 - We can then define the compliance type of an individual
 - The type of an individual describes the level of treatment that an individual would receive given each value of the instrument. So we have $T_i(Z)$

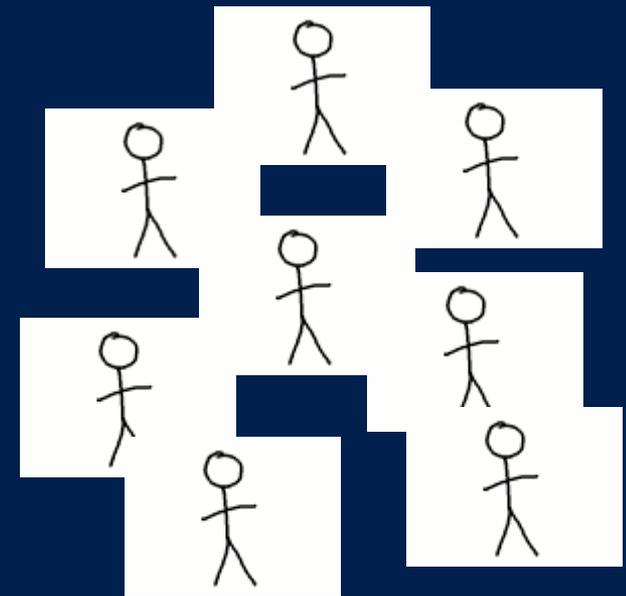


example

- Encouragement design



Treated Village (Z)

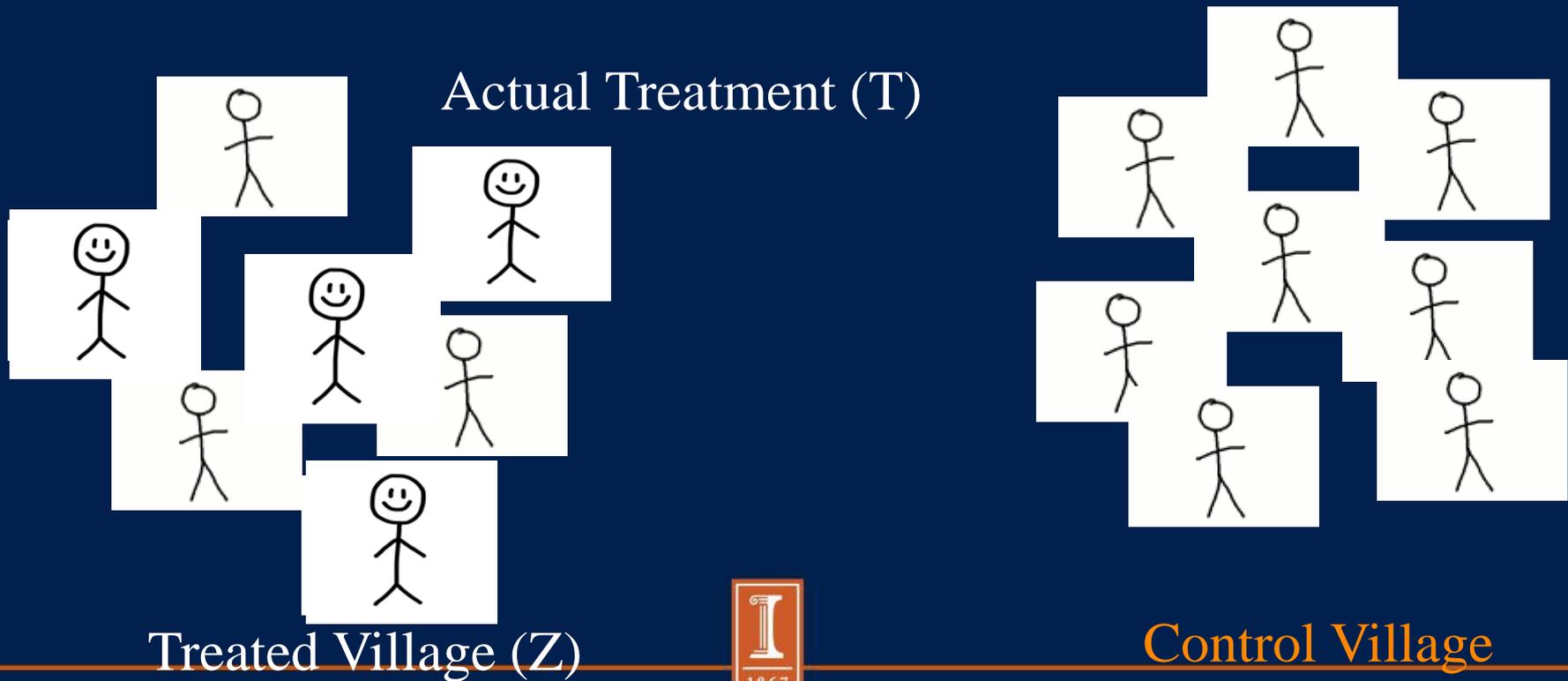


Control Village



example

- Only some people adopt



The Potential Outcomes Approach

- Four types of individuals $T_i(Z)$
 - Never-takers: $T_i(0) = T_i(1) = 0$
 - Compliers: $T_i(0) = 0, T_i(1) = 1$
 - Defiers: $T_i(0) = 1, T_i(1) = 0$
 - Always-takers: $T_i(0) = T_i(1) = 1$

		Z_i	
		0	1
T_i	0	Never-takers/Compliers	Never-takers
	1	Always-takers	Always-takers/Compliers



The Potential Outcomes Approach

- Given the observed data (Z_i, T_i, Y_i) we cannot tell the difference between
 - A complier and an always-taker
 - A complier and an never-taker
- What we require is some additional assumptions that will allow us to identify the complier from the always-taker



The Endogenous Regressor Approach

- When random assignment does not exist and we must use observational data
 - Treatment assignment may not be independent of outcome
 - Ignorability/Unconfoundedness assumption no longer holds
- In the regression context: $Y_i = \alpha + \beta T_i + \epsilon_i$
 - We can no longer assume $Cov(T_i, \epsilon_i) = 0$
 - This violates a principal assumption of OLS



Case 1: Treatment Assignment is Non-Random

- This is endogeneity due to targeting or program placement
- If targeting or program placement is based on observables the solution is easy
 - We can just include the relevant covariates
 - $Y_i = \alpha X_i + \beta T_i + \epsilon_i$
 - By including the relevant covariates in X_i we can ensure that treatment, conditional on those observables, is no longer correlated with the error term



Case 2: Treatment Assignment is Non-Random and Affected by Unobservables

- This is endogeneity due to unobserved heterogeneity
- Including covariates no longer solves the problem
 - Since treatment is dependent on something we cannot observe, that missing or omitted variable ends up in the error term
 - $Cov(T_i, \epsilon_i) \neq 0$
 - In this situation we require a variable that can *instrument for the endogenous treatment* and break correlation between the treatment and the error term



Summary and Discussion

- In both the Potential Outcome Approach and in the Endogenous Regressor Approach we require a set of assumptions and relevant data that will allow us to identify the causal effect.
 - These assumptions are called *Identification Assumptions* and the relevant data are called *Instrumental Variables*
- What are examples of treatment assignment that is not independent of outcomes



What is an IV and How Does it Work?



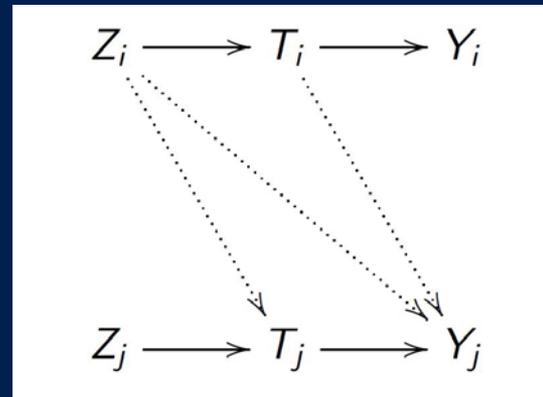
Identification Assumptions

1. SUTVA
2. Exogeneity of the instrument
3. Non-zero average effect of Z on T
4. Monotonic effect of Z on T



1. SUTVA

- Z_i does not affect T_j and Y_j and T_i does not affect Y_j for all $i \neq j$ (non-interference) and there is no (unobserved) variation in the treatment or the instrument.



- The value of my instrument or the status of my treatment does not affect your treatment or your outcome



2. Exogeneity of the Instrument

- All potential outcomes are independent of the instrument

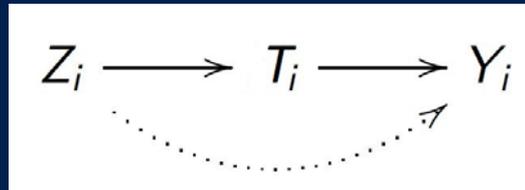
$$(Y_i(0), Y_i(1), T_i(0), T_i(1)) \perp Z_i$$

- This assumption is really made up of two assumptions



2. Exogeneity of the Instrument

- 2A. Ignorability/Unconfoundedness of Z_i
 - Instrument is not correlated with any unobservables that affect the outcome so that its effect on the outcome and treatment received can be consistently estimated
- 2B. Exclusion Restriction



- There is no direct effect of the instrument on the outcome. Any effect of Z_i on Y_i must be through the treatment T_i
- $Cov(Z_i, \epsilon_i) = 0$



3. Non-Zero Average Effect of Z on T

- Instrument must be correlated with treatment

$$\text{Cov}(Z_i, T_i) \neq 0$$



4. Monotonicity

- Increasing the level of the instrument does not decrease the level of the treatment

$$T_i(1) \geq T_i(0) \quad \forall i$$

- This amounts to their being no defiers



Instrumental Variables

- A variable that is a valid instrument for the endogenous treatment is any variable that satisfies the above identifying assumptions
- By using an IV we are able to isolate the part of the treatment variable that is independent of other unobserved characteristics affecting the outcome



One drawback

- Using an IV, we are gaining unbiasedness but losing some efficiency
- In a simple 2-variable case:

$$\text{Var}(\hat{\beta}_{iv}) = \frac{s^2}{n\text{Var}(X)} \frac{1}{\text{corr}(X, Z)^2}$$

$$\text{Var}(\hat{\beta}_{ols}) = \frac{s^2}{n\text{Var}(X)}$$

Why not have a Z that is perfectly correlated with X?



Recap

- But we don't want the correlation between X and Z to be too small
- Recall:
$$\widehat{\beta}_{iv} = \beta + \frac{\text{Cov}(u_i, Z_i)}{\text{Cov}(T_i, Z_i)}$$



Operationalizing IVs



Two-stage least squares (2SLS)

- First, regress treatment on instrument and other exogenous variables

$$T_i = \gamma Z_i + \phi X_i + u_i$$

- Second, calculate the predicted treatment from this regression

$$\hat{T}_i = \hat{\gamma} Z_i + \hat{\phi} X_i$$



Two-stage least squares (2SLS)

- Third, replace T_i with its predicted value \hat{T}_i in to create the reduced form regression equation

$$Y_i = \alpha X_i + \beta(\hat{\gamma}Z_i + \hat{\phi}X_i) + \epsilon_i$$

- In practice we estimate this in a single step

$$Y_i = \alpha X_i + \beta\hat{T}_i + [\epsilon_i + \beta(T_i - \hat{T}_i)]$$

- Note that the standard errors will be wrong



Recap of IV and 2SLS Lingo

- Endogenous variables
 - Independent variables to be instrumented – is correlated with the error term
- Treat an independent variable as endogenous
 - To instrument a variable, meaning to replace it with its fitted values in the second stage of the 2SLS procedure
- Exogenous variables
 - Independent variables (and IVs) that are uncorrelated (orthogonal) with the error term
- Use IV commands to ensure SE are correct



Calculating the LATE

- If we had perfect randomization then we could run the following regression

$$Y_i = \beta T_i + \epsilon_i$$

- Then the Average Treatment Effect is just

$$\beta = ATE$$



Calculating the LATE

- From yesterday: the (LATE) is our IV estimate of the treatment effect

$$\widehat{\beta}_{IV} = \beta + \frac{Cov(u_i, Z_i)}{Cov(T_i, Z_i)}$$

- This is only a local effect because it's the effect of T_i on Y_i for the subpopulation of compliers, and not the whole



The Marginal Treatment Effect (MTE)

- A method for estimating treatment effect when conditional exogeneity does not hold

$$MTE = E[Y_i^T - Y_i^C | X_i = x, U_i = u]$$

- Since the MTE is the limit form of the LATE it defines the treatment effect much more precisely
 - Recall how to calculate it from yesterday



Specification tests



Wu-Hausman Test

- One should test for endogeneity of the treatment
 - First, regress T_i on Z_i and other exogenous covariates, X_i , and obtain the residuals, \hat{u}_i
 - *These residuals reflect all unobserved heterogeneity affecting treatment not captured by the instruments*
 - Second, regress Y_i on X_i , Z_i , and \hat{u}_i
 - *If the coefficient on \hat{u}_i is significant, unobserved characteristics jointly affecting T_i and Y_i are significant then the null that T_i is exogenous is rejected.*
- Note that this test assumes that the IV is valid and is not a test for the validity of the IV



Durbin-Wu-Hausman test

A.k.a. Hausman specification test

$$H = (\hat{\beta}_{ols} - \hat{\beta}_{iv})' (Var(\hat{\beta}_{iv}) - Var(\hat{\beta}_{ols}))^{-1} (\hat{\beta}_{ols} - \hat{\beta}_{iv})$$

- Assumes IV is unbiased
- Compares degree of bias to efficiency loss



Weak instruments

- “Cure can be worse than the disease”
- We don’t want the correlation between X and Z to be too small

$$\widehat{\beta}_{iv} = \beta + \frac{Cov(u_i, Z_i)}{Cov(T_i, Z_i)}$$

Test predictive power in the first stage

F-stat of instrument(s)

For critical values, see (Stock and Yogo 2005)



Sargan-Hansen Test for overidentification

- No test exists to determine if the IV satisfies the exclusion restriction
 - Justification can only be made through direct evidence of how the program and participation evolved
- One can test for overidentifying restrictions
 - First, estimate the structural equation by 2SLS and obtain $\hat{\epsilon}_i$
 - Second, regress $\hat{\epsilon}_i$ on X_i and Z_i and obtain the R^2
 - With a null of no correlation between X_i and $\hat{\epsilon}_i$, test if nR^2 is greater than the critical value. If so then at least one of the instruments is not exogenous



Source of IVs



What Qualifies as a Good IV?

- So, where can you find a good instrument?

“Good instruments come from a combination of institutional knowledge and ideas about the process determining the variable of interest”

-Angrist and Pischke

Mostly Harmless Economics



What Qualifies as a Good IV?

- An IV can be external or randomly assigned but that does not mean the IV is exogenous
- External
 - A variable whose value is set outside of the causal system
 - It is “as good as” randomly determined
- Exogenous
 - A variable that is uncorrelated with (orthogonal to) the error term
 - Satisfies *both* 2A (unconfoundedness/ignorability) *and* 2B (the exclusion restriction)



Discussion of IV Quality

- **Giles and Yoo, 2007, ReStat**
 - Y_i : consumption; T_i : household migrant/network
 - Z_i : Rainfall shocks from distant past
- **Burgess et al., 2012, QJE**
 - Y_i : deforestation; T_i : local government permit to log
 - Z_i : subdividing of local governments
- **Di Falco and Veronesi, 2013, Land Econ**
 - Y_i : Net revenue; T_i : Adaptation strategy
 - Z_i : Access to information sources like extension



Critique: Deaton (2009)

- Instruments: exogenous versus external
 - E.g. rail stations and poverty (river; earthquake)
 - Irrigation dams (land gradient)
 - Child class size; some people don't stay treated (heterogeneous response to instrument)
 - Intent to Treat vs Treatment. Really evaluating those communities/individuals who were induced to change. May not be representative of all communities

